## Using Percentages. \% Stg 6/E7 props \& rats Name:

'Percent' is a word you hear all the time, especially from politicians trying to sell you an idea. E.g. " 51 percent of all dog owners in Levin East agree that all cats should be banned" or "You have a 3 percent chance of being struck by lightning if you dance around outside during a thunderstorm whilst holding an aluminium ladder". But what does 'percent' mean? 'Percent' literally means 'per -hundred' - like there are 100 cents in a dollar. It just shows us a fraction that has been converted to $\mathbf{1 0 0}$ ths. So if I had 3 percent ( $\%$ is the symbol BTW) it is the same as $3 / 100$ ths. Or $51 \%=51 / 100$ ths. And so, like any other fraction 100/100ths, $=1$ and so $100 \%=1$ Let's have a look at some very common percentages:


In fact, knowing that $\mathbf{1 / 1 0}=\mathbf{1 0 \%}$ can help you out of a lot of tricky situations. Figuring out a tenth of any number is easy - just use your old buddy place value to bump it down once. So we can get the percentage of numbers by dividing by 10 , then multiplying by however many we need to again... What? I'll show you:
E.G. what is $\mathbf{4 0 \%}$ of $\mathbf{7 0}$ ? Well, we know that $\mathbf{1 0 \%}$ of $\mathbf{7 0}$ is $\mathbf{7}$. So then we go $\mathbf{4}$ (4 lots of $10 \%$ ) $\mathbf{7} \mathbf{7 = 2 8 \%}$ Try:
a. $60 \%$ of $90=$ $\qquad$ we know $10 \%$ of $90=$ $\qquad$ $\times 6=$ $\qquad$
b. $30 \%$ of $50=$ $\qquad$ we know $10 \%$ of $50=$ $\qquad$ $x 3=$ $\qquad$
c. $90 \%$ of $30=$ $\qquad$ we know $10 \%$ of $30=$ $\qquad$ $x 9=$ $\qquad$
d. $70 \%$ of $80=$ $\qquad$ we know $10 \%$ of $80=$ $\qquad$ $x 7=$ $\qquad$
e. $40 \%$ of $40=$ we know $10 \%$ of $40=$ $\qquad$ $x 4=$ $\qquad$
\% - The modern symbol for percentage came from medieval Italy in the 15th century and evolved over the next two centuries. Earlier, percentages were used in ancient Egypt and India in the fourth century B.C.

By the same logic, it's super easy to figure out what $1 \%$ of any number is too, then we can easily figure other small numbers too! E.G. what is $4 \%$ of $\mathbf{7 0}$ ? $1 \%$ of 70 is 0.7 So then we go $4 \mathbf{x} 0.7=\mathbf{2 . 8 \%}$
f. $6 \%$ of $90=$ $\qquad$ we know $1 \%$ of $90=$ $\qquad$ x $6=$ $\qquad$
g. $3 \%$ of $50=$ $\qquad$ we know $1 \%$ of $50=$ $\qquad$ $\times 3=$ $\qquad$
h. $9 \%$ of $30=$ $\qquad$ we know $1 \%$ of $30=$ $\qquad$ $\times 9=$ $\qquad$
i. $7 \%$ of $80=$ $\qquad$ we know $1 \%$ of $80=$ $\qquad$ x $7=$ $\qquad$
j. $4 \%$ of $40=$ $\qquad$ we know $1 \%$ of $40=$ $\qquad$ $\times 4=$ $\qquad$


Then we can start to join up those parcels of information - we can add the 10s and 1 s to solve some complex ones!
k. $20 \%$ of $90=+\quad+6 \%$ Of $90=$ $\qquad$so
l. $40 \%$ of $50=+\quad+5 \%$ Of $50=$ $\qquad$
m. $50 \%$ of $60=+\quad+3 \%$ Of $60=$ $\square$ so
n. $30 \%$ of $70=\ldots 5 \%$ of $70=$ $\qquad$ so
$35 \%$ of $70=$ $\qquad$

Percentages are just like 100ths, and so closely resemble decimal numbers to 2 places. Have a look at this number line that compares them:


With the number line as a guide, have a go at turning these decimal numbers into percentages:
$0.50=$ $\qquad$ \% $0.25=$ $\qquad$ \%
$0.333=$ $\qquad$ \%
0.99 = ___\%
$0.80=\ldots \%$
$0.666=$ $\qquad$ \% $0.05=\ldots \%$
$0.125=$ $\qquad$ \% $0.40=\ldots$ $0.90=$ $\qquad$
$0.23=$ $\qquad$ \% $0.08=$ $\qquad$ $0.625=$ $\qquad$ \% $0.03=$ $\qquad$ $0.77=$ $\qquad$
$0.52=$ $\qquad$ \% $0.43=\ldots \%$
$0.785=$ $\qquad$ \%
$0.89=\ldots \%$ $0.60=$ $\qquad$
$0.78=$ $\qquad$ \% $0.62=\ldots \%$ $0.44=\ldots \%$ $0.30=$ $\qquad$ \% $1.10=$ $\qquad$ \%
Q. If $100 \%=1$, how can you have $110 \%$ ? A. You need another whole set! Just like you can have $1 \frac{1}{2}$ apples, but you need to start with $\mathbf{2}$ apples.

Here's the thing though, hardly anything in real life is divided up neatly into hundreds. When you do a PAT test at the start of the year, it's 'out of $35^{\prime}$. Your spelling test might be out of 16 or 20 . So how do we figure out what percentage we got? Let's start with some more percentage basic facts:

1. $1 / 4$ of any number $=25 \%$ because $1 \div 4=\mathbf{0 . 2 5}$ so now we know also that 5 out of $\mathbf{2 0}$ is $\mathbf{2 5 \%}$
2. $1 / 2$ of any number $=50 \%$ because $1 \div 2=0.50$
3. $3 / 4$ of any number $=75 \%$ because $(1 \div 4) \times 3=0.75$
4. $1 / 10$ of any number $=10 \%$ because $1 \div 10=\mathbf{0 . 1 0}$
5. $1 / 3$ of any number $=33.3 \%$ because $1 \div 3=\mathbf{0 . 3 3 3 r}$ so now we know also that $\qquad$ out of 30 is $\mathbf{3 3 . 3 \%}$
6. $1 / 5$ of any number $=20 \%$ because $1 \div 5=\mathbf{0 . 2 0}$
7. $1 / 8$ of any number $=12.5 \%$ because $1 \div 8=\mathbf{0 . 1 2 5}$
8. $2 / 3$ of any number $=66.6 \%$ because $(1 \div 3) \times 2=0.666$
9. $3 / 5$ of any number $=60 \%$ because $(1 \div 5) \times 3=0.60$
10. $4 / 5$ of any number $=80 \%$ because $(1 \div 5) \times 4=\mathbf{0 . 8 0}$
so $25 \%$ of $20=5$
so $50 \%$ of $60=$ $\qquad$
so $75 \%$ of $20=$ $\qquad$
so $10 \%$ of $70=$ $\qquad$
so $33.3 \%$ of $30=$ $\qquad$
so $20 \%$ of $20=$ $\qquad$
so $12.5 \%$ of $80=$ $\qquad$ so $66.6 \%$ of $60=$ $\qquad$ so $60 \%$ of $50=$ $\qquad$
so $80 \%$ of $100=$ $\qquad$ so now we know also that $\qquad$ out of 100 is $\mathbf{8 0 \%}$
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We've learned some basic facts about percentages, but what if the numbers are a little trickier - say like figuring out what percentage 5 out of 12 is, or 7 out of 11 . Let's have a look.

5 out of $\mathbf{1 2}$ as a percentage: First we'll need to use our fast long-division skills to chop $\mathbf{5}$ into $\mathbf{1 2}$ bits. (Yes, that's right) We want to end up a decimal version of our fraction - the test had 12 questions, or parts, and we are talking about 5 of those parts. $(5 \div 12) \times 100=? ? ?$
$\begin{array}{ll}0.416 \mathrm{r} & \text { Now all you have to do is multiply the quotient (division answer) by } 100 \\ 1 2 \longdiv { 5 ^ { 5 } 0 ^ { 2 } 0 ^ { 8 } 0 ^ { 8 } } & 0.417 \times 100=41.7 \\ 5^{2} & \text { so: } 5 / 12=41.7 \%\end{array}$ Try some (mmm tasty):

| $7 / 11$ | $1 1 \longdiv { 7 . 0 0 0 }$ | $\times 100=\_\%$ |
| :--- | :--- | :--- |
| $5 / 8$ | $8 \longdiv { 5 . 0 0 0 }$ | $\times 100=\_\%$ |
| $13 / 20$ | $2 0 \longdiv { 1 3 . 0 0 0 }$ | $\times 100=\_\%$ |
| $7 / 9$ | $9 \longdiv { 7 . 0 0 0 }$ | $\times 100=\ldots \%$ |

How though, would I work percentages out on a calculator? (I know you want to) easy! Say I need a percentage for 28 out of 90. Punch in ' 28 '. Press ' $\div$ ' then put in ' 90 $=$ ' you should get a decimal like 0.31111111 - you don't need all those 1 s , just use the first 2 or 3 decimal places: 0.311 , then press ' $x 100=$ ' and you'll see your percentage: 31.1

Maths inquiry - Work with a buddy if you like - use your maths book to do the working out.
Some wordy word questions like you find in annoying maths tests full of words:
a. $10 \%$ of our class have blonde hair. One boy and two girls. How many kids are in our class? $\qquad$
b. $50 \%$ of everyone in Hamilton metropolis owns a pair of gumboots. 180 thousand people live there - how many people own gumboots? $\qquad$
c. In my bowl there are 12 pieces of fruit. 3 of them are apples - what percentage of apples is there?
$\qquad$ \%
d. A recent survey said that $75 \%$ of all people prefer doughnuts over Brussel sprouts. They asked 120 people how many of them prefer doughnuts? $\qquad$
e. If I have 30 blue marbles, 20 green, 40 red ones and 10 yellow ones, what percentage of my marbles are green? $\qquad$ \%
f. I did a maths test on proportions and ratios and got 18 out of 24 correct. What was my percentage?
$\qquad$ \%
g. A factory making pooper-scoopers had a product failure rate of $1 \%$. Last year they made 100000 scoopers - how many failed? $\qquad$
h. Every $3^{\text {rd }}$ person you meet in a group of 366 people is wearing clown shoes. What percentage of them are NOT wearing clown shoes? $\qquad$ \%
i. $12 \%$ of boys ride skateboards, $30 \%$ of boys ride bikes, $25 \%$ get dropped off. The rest just walk. What percentage of boys have to walk? $\qquad$ \%
j. In a large family with 11 kids (poor mum) 8 are girls. What percentage of the kids are boys? $\qquad$ \%
k. It's easy to work out what $10 \%$ of 428 is right? So, using that knowledge, figure these out: $15 \%$ of $428=$
$40 \%$ of $428=$ $\qquad$ $25 \%$ of $428=$ $\qquad$


[^0]:    "If there is a 50-50 chance that something can go wrong, then 9 times out of ten it will".

